

Mathematics (Economics, Markets and Finance)

Luciano Battaia - Mesfin Geremew Genie

Exercises sheet 3

Exercise 1. Find the following integrals:

a) $\int 9\sqrt[3]{x} \, dx;$

b) $\int \frac{2}{\sqrt[5]{x}} \, dx;$

c) $\int \frac{x}{\sqrt[7]{x^3}} \, dx;$

d) $\int 8x^2\sqrt[7]{x^5} \, dx;$

e) $\int \frac{1}{x^2\sqrt[3]{x^2}} \, dx.$

Exercise 2. Find the following integrals:

a) $\int \frac{1}{x-1} \, dx;$

b) $\int \frac{1}{5+2x} \, dx;$

c) $\int \frac{x}{1+x^2} \, dx;$

d) $\int \frac{2x+1}{x^2+x+9} \, dx;$

e) $\int \frac{x^2}{x^3+2} \, dx;$

f) $\int \frac{x+1}{x^2+2x+5} \, dx.$

g) $\int \frac{e^x}{e^x+1} \, dx.$

Exercise 3. Find the following integrals:

a) $\int 2xe^{x^2} dx;$

b) $\int e^{-x} dx;$

c) $\int x^2 e^{-x^3} dx;$

d) $\int (2x + 3)e^{x^2+3x} dx.$

Exercise 4. Find the following integrals:

a) $\int (e^{2x} + x^3 + \sqrt{x}) dx;$

b) $\int \frac{x^2 + 2}{x^3} dx;$

c) $\int (x^2 + x\sqrt{x} + xe^{x^2}) dx;$

d) $\int \frac{x^2 + 1}{x\sqrt{x}} dx$

Exercise 5. Find the following integrals:

a) $\int \ln x dx;$

b) $\int xe^x dx;$

c) $\int xe^{-x} dx;$

d) $\int x^2 e^x dx.$

Exercise 6. Calculate the area between the given functions, the x axis and the two vertical lines given.

a) $f(x) = e^x, x = 0, x = 2.$

b) $f(x) = x^2 + 1, x = 1, x = 3.$

c) $f(x) = \ln x, x = 1, x = e.$

d) $f(x) = \sqrt{x}, x = 1, x = 4.$

Exercise 7. Given the function

$$f(x) = \begin{cases} x^2, & \text{if } x < 1; \\ -x + 2, & \text{if } x \geq 1; \end{cases}$$

calculate the area between the graph, the x axis and the vertical lines $x = 0$ and $x = 2$.

Exercise 8. Calculate the area between the graphs of the following functions:

a) $f(x) = x^2$ and $g(x) = x$;

b) $f(x) = x^2 - 1$ and $g(x) = -x^2 + x$.

Exercise 9. Find the following improper integrals, if they converge.

a) $\int_0^{+\infty} e^{-x} dx$;

b) $\int_1^{+\infty} \frac{1}{x^2} dx$;

c) $\int_{-\infty}^1 e^x dx$;

d) $\int_0^1 \frac{1}{\sqrt{x}} dx$;

e) $\int_0^1 \frac{1}{x^2} dx$;

f) $\int_1^{+\infty} \frac{1}{x} dx$.